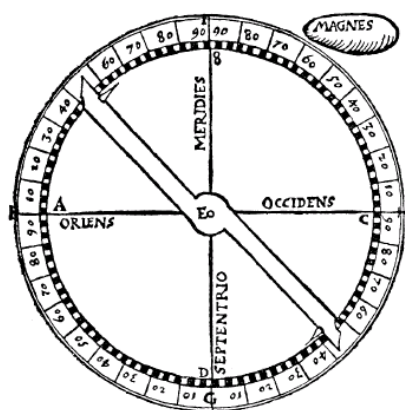


GeoForschungsZentrum Potsdam

Geomagnetic Results Wingst

2000

Yearbook No. 46



Potsdam 2004



Wingst Observatory: The Absolute House on the left and the Variometer House in the background



FGE double system at Wingst Observatory. One of the suspended triples is provided with a coil system constructed after Beblo et al. (1999)

Cover: Compass after Pierre de Maricourt, 1269 (SCHÜCK, 1911)

Geomagnetic Results Wingst 2000 – Yearbook No 46

Günter Schulz

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| 1 | Introduction | |

This report (yearbook No 46) contains the results of Erdmagnetisches Observatorium Wingst (WNG) for 2000. Earlier reports were published by Bundesamt für Seeschifffahrt und Hydrographie¹).

The enclosed CDrom contains recorded minute values as well as derived (hourly, daily, monthly) mean values and indices. It also provides recalculated epoch values from 1939.5 on and those of Marineobservatorium Wilhelmshaven (WLH) before then. Revised sets of monthly and daily mean values (since 1943) and K values (since 1944) are also included.

Using the visualisation software year.exe, the one-minute, hourly and daily values of the year under review can be displayed as graphs in the same manner as in the years before. High resolution magnetograms for each day are stored as post script files on the CDrom.

In the year under review, Wingst Observatory additionally published on a monthly basis:

- a) Reports on geomagnetic indices and special geomagnetic events
- b) Reports on preliminary daily and monthly means

Geomagnetic data have been provided on a regular basis to the following institutions:

- a) International Space Environment Service (ISES): Geomagnetic indices and geomagnetic events (daily)
- b) International Service of Geomagnetic Indices (ISGI): Geomagnetic indices and special geomagnetic events (monthly and annually)
- c) World Data Centers for Geomagnetism: Microfiches of pulsation magnetogrammes, geomagnetic indices and one-minute values (annually)
- d) INTERMAGNET (Global near-real-time magnetic observatory network): One-minute values (reported data via METEOSAT and Email, hourly; adjusted data via Email, on weekdays); Geomagnetic indices and one-minute values (CDrom, annually)

¹ The last one of these reports (SCHULZ, 2004) contains a complete digital set of all data that have been published since the establishment of Wingst Observatory in 1938.

Indices and information about special events were made available through a telephone service on weekdays.

Phone: +49 4778 812152

The preliminary variations and indices can be found on the Internet on a real time basis (10 min updates) in graphical form:

http://www.gfz-potsdam.de/pb2/pb23/GeoMag/Other/BothObs_e.html

or (update every hour):

<http://www.bsh.de/en/Marine%20data/Observations/Geomagnetism/obs.jsp>

and in numerical form (update every 10 minutes, pass word required):

<ftp://wng@ftp.bsh.de/outgoing/boulder>

Definitive (compressed) data from 1939 onwards (minute values since 1981) can be found at:

<ftp://ftp.bsh.de/outgoing/wng>

The following list shows some additional selected links providing Wingst data:

Intermagnet (variations):

<http://www.intermagne.bgs.ac.uk/cgi-bin/imagform>

RWC Brussels (indices):

<http://sidc.oma.be/products/wng/index.php3>

WDC Kyoto (pulsations):

<http://swdccb.kugi.kyoto-u.ac.jp:80/film>

WDC Copenhagen (variations):

<http://web.dmi.dk/fsweb/projects/wdcc1/obs.html>

Address for data requests, data exchange and information:

Erdmagnetisches Observatorium
Am Olymp 13
D-21789 Wingst

Phone: +49 4778 812110

Fax: +49 4778 812150

E-mail: guenter.schulz@bsh.de

Collaborators: W.D. Grube and A. Glodek.

2 General Remarks

Wingst Geomagnetic Observatory was established in 1938 as a successor to Wilhelmshaven. Since then, the station has been operated without interruption. The observatory's development is described by VOPPEL, 1988, and SCHULZ, 2001 (see also appendix 3). The development of the modern recording devices is given by SCHULZ, 1998. For the instrumentation since 1938, see also instr.txt on the Cdrom.

The observatory is located in the Lower Elbe area on top of a terminal moraine of the Saale glacial period (elevation 50 m). Its co-ordinates are:

| | Latitude | Longitude |
|-------------|------------|------------|
| Geographic | 53° 44.6'N | 09° 04.4'E |
| Geomagnetic | 54.2° | 95.3° |

Geomagnetic co-ordinates refer to DGRF (Definitive Geomagnetic Reference Field) 1980.

The following abbreviations are used throughout this report:

- X North component
- Y East component
- Z Vertical component (downward positive)
- H Horizontal intensity
- D Declination (eastward positive)
- I Inclination (downward positive)
- F Total intensity
- U North-west component
- V North-east component

Times are related to UTC (Co-ordinated Universal Time).

2.1 Recording systems

The results of this edition were derived from the following recording systems:

- a) Digital system for variations:

Suspended fluxgate magnetometer (FM) of type FGE(DMI) (U, V, Z): One-minute and hourly means as well as indices of activity
Proton precession magnetometer (PPM) of type V75(VARIAN) (F): One minute spot values for quality check only

- b) Photographic system for variations of type SCHULZE/LA COUR (D , H and Z ; 20 mm h^{-1}): Geomagnetic events (ssc, sfe, bay) and substitute hourly means
- c) Photographic system for pulsations of type KIM762(KARMANN) (amplitude and phase characteristics see yearbook 1984): Geomagnetic events (pc, pi)

2.2 Levels, standards and constants

The results of this edition refer to the International Magnetic Standard (IMS). The results of the yearbooks up to and including 1980 referred to the Observatory Standard (OBS), which was represented by the classic type base line instruments bound to their original locations and surroundings.

H , Z , and F are referred to the proton vector magnetometer (PVM) of type ASKANIA/V4931(VARIAN) on pier NW (section 3.2), D to the fluxgate theodolite (DI-flux) of type 010B(ZEISS)/MAG01H(BARTINGTON) on pier NE (section 3.1) of the absolute house. Both instruments are assumed to represent IMS.

The following equations apply to D (see yearbook No 37, 1991), H and Z (see yearbook No 38, 1992):

$$\begin{aligned} D_{OBS} &= D_{IMS} \\ H_{OBS} &= H_{IMS} + 6.7 \text{ nT} \\ Z_{OBS} &= Z_{IMS} + 11.1 \text{ nT}. \end{aligned}$$

The differences for the derived elements depend on the components, i.e. for 2000:

$$\begin{aligned} F_{OBS} &= F_{IMS} + 12.8 \text{ nT} \\ I_{OBS} &= I_{IMS} - 0.15' \\ X_{OBS} &= X_{IMS} + 6.7 \text{ nT} \\ Y_{OBS} &= Y_{IMS} \end{aligned}$$

The following physical standards are available at Wingst. They guarantee the quality of data:

SCHWILLE (frequency, DCF77, 10^{-8})
 PATEK PHILIPPE and HOPF (UTC, DCF77)
 CROPICO VS10 (Voltage, $5 \cdot 10^{-6}$)
 GUILDLINE 100 Ohm (resistance, $5 \cdot 10^{-6}$)
 Helmholtz coil of high precision (magnetic field strength, 10^{-4})

For the determination of the magnetic induction, the IAGA-recommended gyromagnetic constant (RASMUSSEN, 1991) was used:

$$2\pi\tau^{-1} = 23.487203 \text{ nT s}$$

The azimuth marks were last checked by the German Geodetic Survey in 1995. Their values, related to the NE pier (R: 3504926.873, H: 5956702.028), and their deviations in the year under review are:

| Azimuth mark | Azimuth | Deviation against |
|--------------|-------------|-------------------|
| N | 3811° .36' | N |
| NE | 13° 23.19' | (-0.14 ±0.04)' |
| W | 308° 42.94' | (-0.01 ±0.03)' |

2.3 Special measurements

In the year under review, comparative measurements were carried out at Wingst and at the observatories Fürstenfeldbruck (FUR), Hurbanovo (HRB) and Wien-Kobenzl (WIK). The station differences are as follows:

| at | WNG minus | D | I | F |
|-----|-----------|--------|--------|---------|
| FUR | FUR | -0.19' | -0.05' | 0.0 nT |
| HRB | HRB | +0.01' | -0.06' | +0.1 nT |
| WIK | WIK | -0.25' | +0.07' | +1.5 nT |
| WNG | NGK | -0.07' | -0.12' | -1.0 nT |

3 Absolute measurements

The absolute measurements were reduced according to the variations of the digital system (section 4).

3.1 Declination and Inclination

Absolute measurements of D were made with the DI -flux on an approximately monthly basis. Also the determination of I was included in the measurement routine. Each measurement is based on a set of four positions. I was corrected by the pier difference of $-0.2'$ in the sense of NW minus NE. The differences $E=I-\arctg(Z/H)$ are shown in Table 1.

Additionally, relative measurements of D were carried out with the PVM according to the addition field method (Serson) on a weekly basis. The mean difference in the sense of PVM minus DI -flux of all pairs of measurements carried out on the same day was used as an instrument constant. Its value e is as follows:

$$e = -23.88' \text{ (11 measurements).}$$

3.2 Horizontal intensity, vertical component and total intensity

Absolute measurements of H and Z were carried out with the PVM according to the compensation field method (Nelson) after each relative determination of D .

The magnetic induction vector is over-determined due to the measurement of three elements within the meridian plane. The difference $c = F - (H^2 + Z^2)^{1/2}$ represents the measurements' inherent accuracy. The annual mean of the error c amounted to:

$$+0.5 \text{ nT} \pm 0.4 \text{ nT value (52 measurements).}$$

C is shown in Table 1.

As a rule, the PPM of type V75 was used. This instrument shows a long-term drift of some 0.1 nT depending on the components (SCHULZ AND CARSTENS, 1979). Therefore, comparative measurements using the PPM of type V4931, which represents IMS (see section 2.2), were carried out on a monthly basis. All base line values as well as the recorded minute spot values of F (section 4) are referred to this instrument.

4 Digital recording system

Minute mean values of the orthogonal components U , V , and Z as well as spot values of F were acquired by the primary digital system (V75 and FGE (No 125), section 2.1). The PPM is not only part of the recording system but also serves as an indicator of the PVM (section 3).

Owing to over-determination, outliers, jumps and short-term base line instabilities between the dates of absolute measurements of all three components could be detected (section 4.1) and, under certain conditions, automatically eliminated. The following equation applies to Wingst:

$$dF = 0.26 dU + 0.26 dV + 0.93 dZ.$$

Additionally, a fourth fluxgate was operated, which had been aligned in such a way that its W orientation satisfies the following equation:

$$dW = 0.578(dU + dV + dZ).$$

In this way, jumps and outliers of the secondary system could be monitored independently.

A second suspended FM of type FGE (No 126), an FM of type EDA FM100B and a PPM of type PPM105(EDA) were operated as stand-by devices in case of failure of the primary system.

4.1 Base line values

Table 1 shows the base line values of the FGE125 referred to IMS. Fig 1 shows the results in graphical form. Absolute measurements of D and I (DI-flux) are marked by circles, those of H and Z (PVM) as well as relative measurements of D by dots. I (derived from H and Z) is also displayed (dots).

To obtain base line values, the dependence of the measured elements D , H , I and F on the recorded components U , V , and Z within the range of variations was developed up to terms of second order (section 6). Minute mean values of the magnetometer and the baseline instruments were processed, which had been synchronized within ± 5 s.

For 2000, the base line values of the primary components refer to the following equivalent voltages E of the fluxgate compensation fields:

| Component | E in mV (nominal) |
|-----------|---------------------|
| U | 12861 |
| V | 12613 |
| Z | 45463 |

4.2 Scale values, temperature coefficients and cross talk

Scale values and cross talk were traced back to the respective parameters of the old FM100C(EDA) system by employing stochastic methods, making use of strong variations during a substorm on April 7, 1995 (SCHULZ, 1998). The following values apply to the primary components (FGE125):

| | Scale Values in nT/mV 1.000+ | Cross Talk against FM100C in 10^{-3} | |
|-----|---------------------------------|--|-------------------|
| U | $+10^{-3}(1.4 \pm 0.6)$ | $V: +0.2 \pm 1.0$ | $Z: +0.9 \pm 0.6$ |
| V | $-10^{-3}(1.5 \pm 0.8)$ | $U: -0.7 \pm 0.6$ | $Z: -0.5 \pm 0.4$ |
| Z | $+10^{-3}(0.8 \pm 0.6)$ | $U: -0.6 \pm 0.4$ | $V: -1.2 \pm 0.8$ |

Considering the respective values of the FM100C (see yearbook No 41, 1995), the absolute misalignments and errors of the scale values of the FGE125 fluxgates probably do not exceed the order of magnitude of 10^{-3} .

Temperature coefficients were neglected because the FGE double system had been installed in the old variometer room (SCHULZ 2001) with almost perfect temperature control (contact thermometers, $\pm 0.03^\circ\text{C}$).

5 Data processing

The base line values (Tables 1) were smoothed by Bathspline approximation in steps of 0.01' for *D* or 0.1 nT for *H* and *Z*, respectively (SCHOTT, 1992).

Hourly mean values were formed using 60 minute mean values of *U*, *V*, and *Z* (taken at minutes 00 to 59 UTC and centred at second 30) as well as 60 *F* spot values (taken at second 05).

The international quiet (*Q*) and disturbed (*D*) days were taken from the Niemegek listings of ISGI. *A* denotes normal days. In the case of averaging, *A* means that all days of the month or the year, respectively, have been included.

The data were processed by a computer double system of type HP9000 330/360. Each workstation is connected to a data acquisition unit of type HP3852 and to the Internet. All necessary calculations including those for the yearbook were carried out by the workstation of type HP9000 360.

6 Indices

The indices presented in this edition (File wng00.k and Table 4) indicate the local disturbances of the geomagnetic field resulting from particle radiation. Their meaning in detail:

K: geomagnetic three-hourly index, quasi-logarithmic measure of the maximum disturbance in steps of 0 to 9; lower limit for *K* = 9: 500 nT

sum: Sum of the eight three-hourly indices of a day

Ak: Mean value of the equivalent amplitudes derived from the eight three-hourly indices. The mean value of the daily disturbance of the geomagnetic field is 2 *Ak* nT

Ck: daily character figure derived from *Ak* and scaled from 0.0 to 2.5.

C: estimated daily character figure; scale: 0, 1, 2

The indices were derived using the IAGA-recommended FMI-routine (Häkkinen, 1992).

7 Files on the CDrom

| | |
|--|--|
| <i>\wingst\</i> <i>subdirectories and files</i> | <i>Wingst root directory, containing the following</i> |
| tree_00.txt: | File structure |
| info.txt: | Information on the operating system |
| <i>yearb00\:</i> | <i>Directory containing this report (yearbook No 46), tables 5 and 6, magnetograms and a reprint</i> |
| yearb00\yearb00.pdf: | This report |
| yearb00\tabs5_00\: | Directory containing tables wngYYmmm.e of hourly and daily mean values for the month mmm of the element e data (<i>D</i> in 0.1', <i>H</i> and <i>Z</i> in nT). |
| yearb00\tabs6\tab6_00.txt: | Tables of indices |
| yearb00\mags00\dhz2000mmdd.ps: | Magnetograms (post script) of the day dd in the month mm |
| yearb00\instr.txt: | Instruments used since 1938 |
| yearb00\wng6dec.pdf: | Reprint of SCHULZ, 2001 |
| <i>progs\:</i> | <i>Directory containing software</i> |
| progs\year.exe: | Visualisation programme for hourly and daily mean values as well as one-minute values located in data\2000 |
| progs\readme.txt: | Notes concerning operation of the programme year.exe and the meaning of the parameters in year.ini |
| progs\setup.bat: | Installs the programme year under the local directory c:\year and starts the visualisation software |
| <i>data00\:</i> | <i>Directory containing the following data</i> |
| data00\wlh+wng.yr: | Updated epoch values WLH and WNG (<i>D</i> and <i>I</i> in 0.1'; <i>F</i> , <i>H</i> , <i>X</i> , <i>Y</i> , and <i>Z</i> in nT) |
| data00\wng.mon: | Updated monthly mean values WNG (since 1943; <i>D</i> and <i>I</i> in 0.1'; <i>F</i> , <i>H</i> , <i>X</i> , <i>Y</i> , and <i>Z</i> in nT) |

data00\wng.day: Updated daily mean values WNG (since 1944; *D* and *I* in 0.1'; *F*, *H*, *X*, *Y*, and *Z* in nT)

data00\wng.k: Updated activity figures *K*, *Ak*, *Ck*, and *C* as well as monthly and annual mean values of *Ak*, *Ck*, and *C* (since 1944)

yearb.exe input files:

data00\hour00\wng00mmm.wdc: Hourly mean values of the month *mmm* in the format WDC (ICSU, 1989); *yearb.exe* input files

data00\min00mm\wng00mmm.0nn: One-minute values of the days *nn* for the month *mm* or *mmm*, respectively, in the format WDC (ICSU, 1989); *yearb.exe* input files

data00\iaga00\: Directory containing the following data in the IAGA2000 format (<http://www.ngdc.noaa.gov/IAGA/wg2>)

data00\iaga00\YR.WNG: Epoch values WNG starting 1939 (from 1981 on: *D* and *I* in 0.01'; *X*, *Y*, *Z*, *H* and *F* in 0.1 nT; before then: 0.1' or 1 nT, respectively)

data00\iaga00\2000MT.WNG: Monthly means (*D* and *I* in 0.01'; *X*, *Y*, *Z*, *H* and *F* in 0.1 nT)

data00\iaga00\2000DY.WNG: Daily means (*D* and *I* in 0.01'; *X*, *Y*, *Z*, *H* and *F* in 0.1 nT)

data00\iaga900\2000mmHR.WNG: Hourly means (*F*, *X*, *Y* and *Z* in 0.1 nT) of the month *mm*

data00\iaga00\2000mmMN.WNG: Minute means (*F*, *X*, *Y* and *Z* in 0.1 nT) of the month *mm*

8 References

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Appendix 1 and 2: Figures and Tables

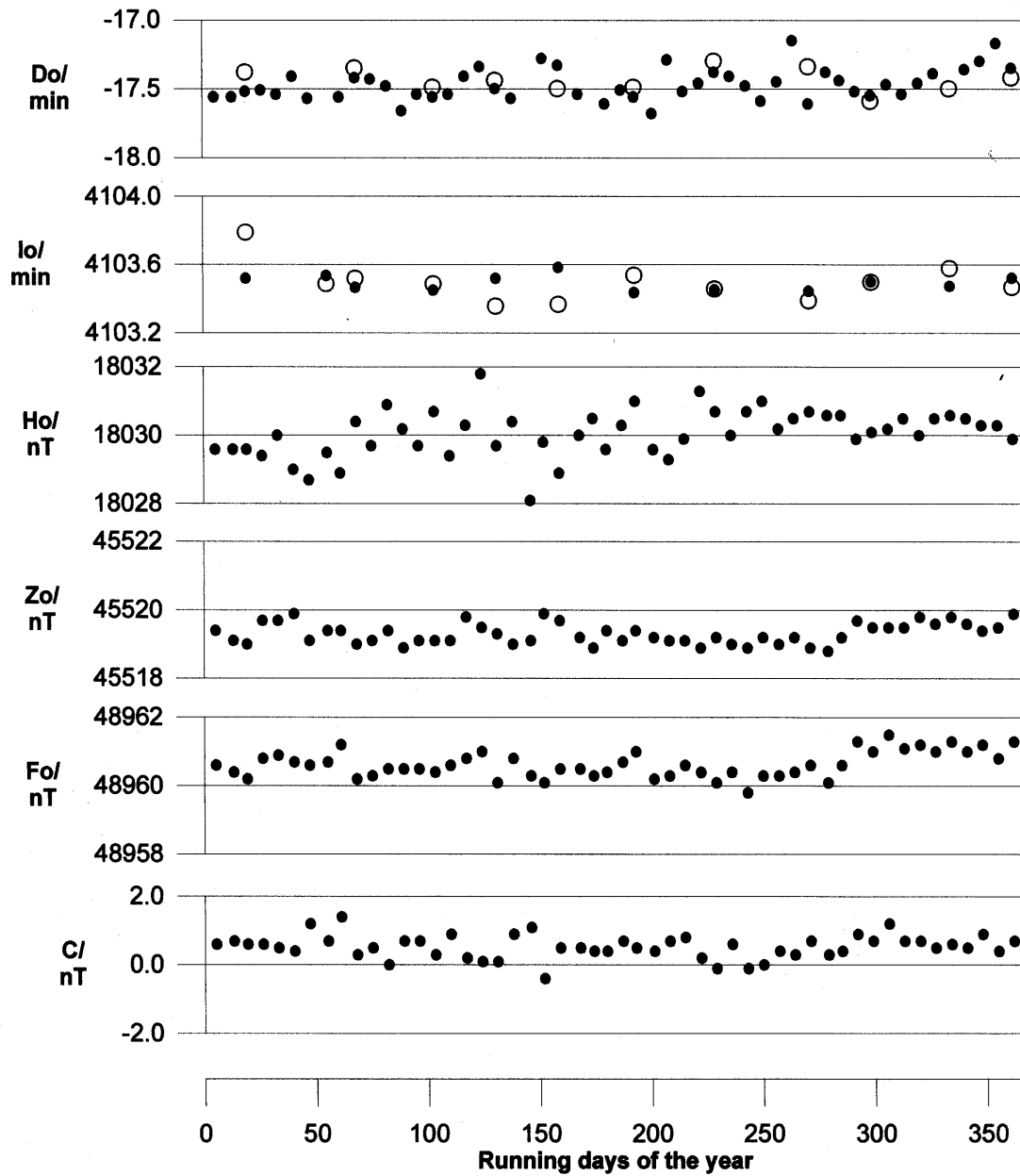


Fig. 1

Wingst 2000 Base line values of the fluxgate system FGE125, IMS

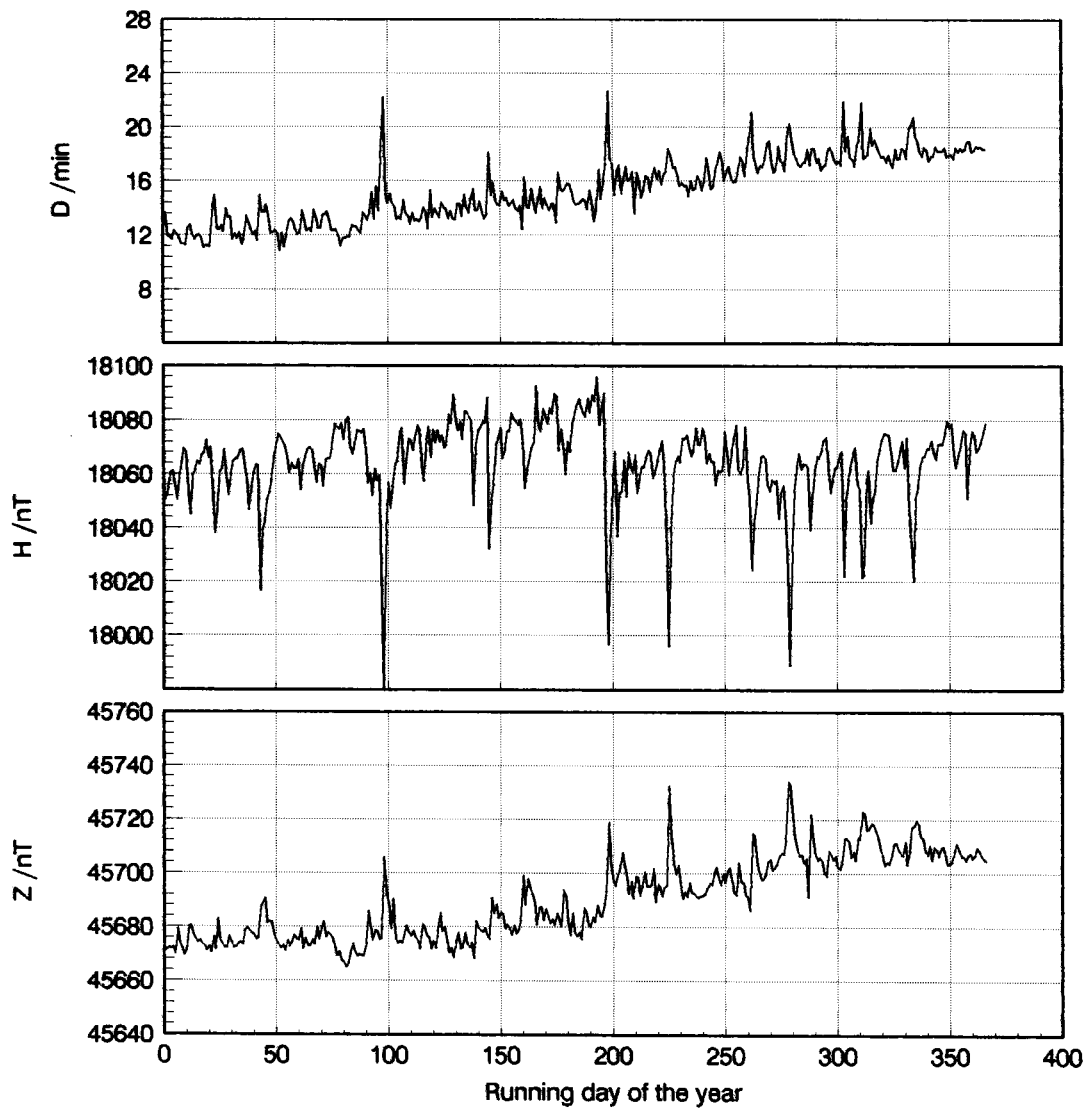


Fig. 2

Wingst 2000 Daily mean values D , H and Z

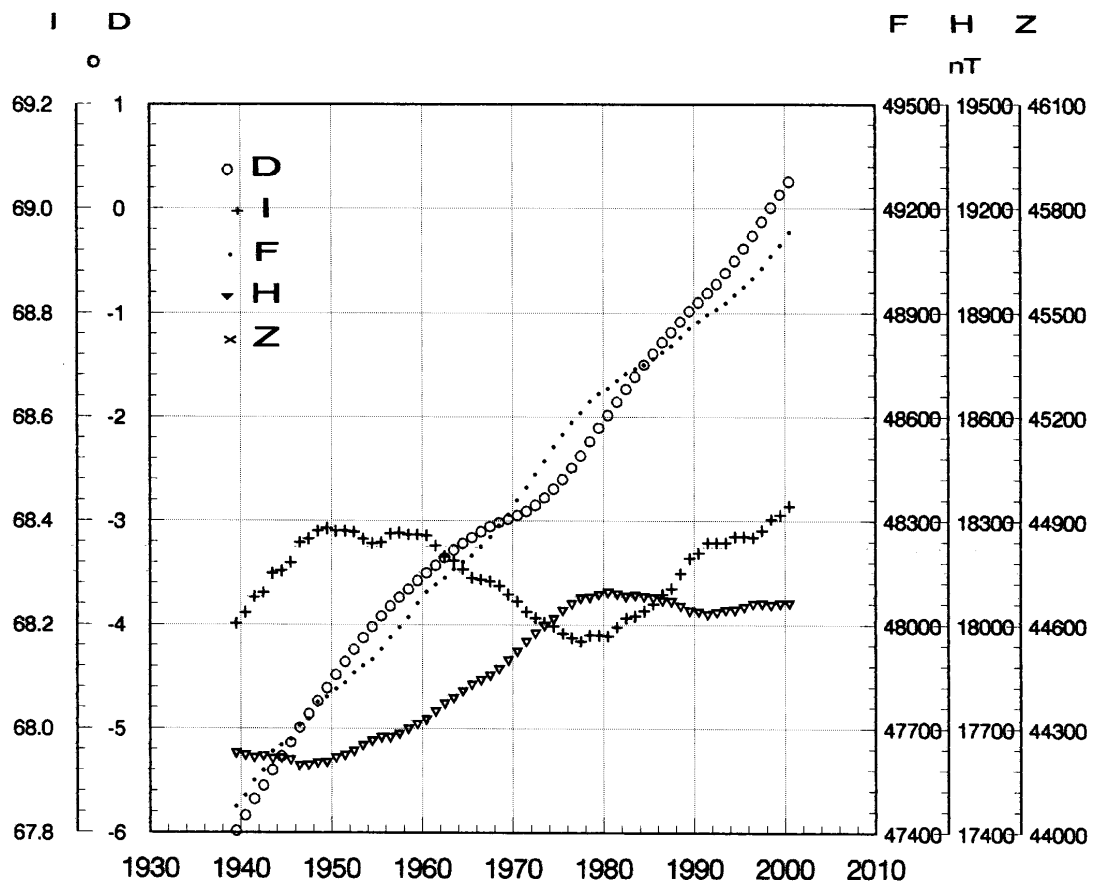


Fig. 3

Wingst Epoch values I, D, F, H and Z

```

wingst\
  tree_00.txt
  info.txt
  yearb00\
    yearb00.pdf
    tabs5_00\
      wng00jan.d
      wng00jan.h
      wng00jan.z
      .
      wng00dec.d
      wng00dec.h
      wng00dec.z
    tab6_00.txt
    mags00\dhz20000101.ps
    .
    mags00\dhz20001231.ps
    instr.txt
    wng6dec.pdf
  progs\
    readme.txt
    year.exe
    year.ini
    setup.bat
    att.bgi
    cga.bgi
    egavga.bgi
    herc.bgi
    vesal6.bgi
  data00\
    wlh+wng.yr
    wng.mon
    wng.day
    wng.k
    hour00\
      wng00jan.wdc
      .
      wng00dec.wdc
    min0001\
      wng00jan.001
      .
      wng00jan.031
      .
    min0012\
      wng00dec.001
      .
      wng00dec.031
    iaga00\
      YR.WNG
      2000MT.WNG
      2000DY.WNG
      200001MT.WNG
      .
      200012MT.WNG
      200001HR.WNG
      .
      200012HR.WNG

```

Fig. 4

Structure of the file set on CDrom

Wingst 2000

Base-line measurements, system FGE125, IMS

| Month | day | Do(abs) | Do(rel) | Io | Fo nT | Ho nT | Zo nT | C | E |
|-------|-----|-----------|-----------|------------|----------|----------|----------|------|--------|
| Jan. | 5 | | -0°17.56' | | 48960.6 | 18029.6 | 45519.4 | +0.6 | |
| | 13 | | -0 17.56 | | 48960.4 | 18029.6 | 45519.1 | +0.7 | |
| | 19 | -0°17.38' | -0 17.52 | +68°23.79' | 48960.2 | 18029.6 | 45519.0 | +0.6 | +0.27' |
| | 26 | | -0 17.51 | | 48960.8 | 18029.4 | 45519.7 | +0.6 | |
| Feb. | 2 | | -0 17.54 | | 48960.9 | 18030.0 | 45519.7 | +0.5 | |
| | 9 | | -0 17.41 | | 48960.7 | 18029.0 | 45519.9 | +0.5 | |
| | 16 | | -0 17.57 | | 48960.6 | 18028.7 | 45519.1 | +1.2 | |
| | 24 | | +* 39.99 | +68 23.49 | 48960.7 | 18029.5 | 45519.4 | +0.7 | -0.05 |
| March | 1 | | -0 17.56 | | 48961.2 | 18028.9 | 45519.4 | +1.5 | |
| | 8 | -0 17.35 | -0 17.42 | +68 23.52 | 48960.2 | 18030.4 | 45519.0 | +0.3 | +0.05 |
| | 15 | | -0 17.43 | | 48960.3 | 18029.7 | 45519.1 | +0.5 | |
| | 22 | | -0 17.48 | | 48960.5 | 18030.9 | 45519.4 | +0.0 | |
| | 29 | | -0 17.66 | | 48960.5 | 18030.2 | 45518.9 | +0.7 | |
| April | 5 | | -0 17.54 | | 48960.5 | 18029.7 | 45519.1 | +0.7 | |
| | 12 | -0 17.49 | -0 17.56 | +68 23.49 | 48960.4 | 18030.7 | 45519.1 | +0.3 | +0.04 |
| | 19 | | -0 17.54 | | 48960.6 | 18029.4 | 45519.1 | +0.9 | |
| | 26 | | -0 17.41 | | 48960.8 | 18030.3 | 45519.8 | +0.2 | |
| May | 3 | | -0 17.34 | | 48961.0 | 18031.8 | 45519.5 | +0.1 | |
| | 10 | -0 17.44 | -0 17.50 | +68 23.36 | 48960.1 | 18029.7 | 45519.3 | +0.2 | -0.16 |
| | 17 | | -0 17.57 | | 48960.8 | 18030.4 | 45519.0 | +0.9 | |
| | 25 | | 48960.3 | 18028.1 | 45519.1 | +1.1 | | | |
| | 31 | | -0 17.28 | | 48960.1 | 18029.8 | 45519.9 | -0.4 | |
| June | 7 | -0 17.50 | -0 17.33 | +68 23.37 | 48960.5 | 18028.9 | 45519.7 | +0.5 | -0.21 |
| | 16 | | -0 17.54 | | 48960.5 | 18030.0 | 45519.2 | +0.5 | |
| | 22 | | 48960.3 | 18030.5 | 45518.9 | +0.4 | | | |
| | 28 | | -0 17.61 | | 48960.4 | 18029.6 | 45519.4 | +0.4 | |
| July | 5 | | -0 17.51 | | 48960.7 | 18030.3 | 45519.1 | +0.7 | |
| | 11 | -0 17.49 | -0 17.56 | +68 23.54 | 48961.0 | 18031.0 | 45519.4 | +0.5 | +0.10 |
| | 19 | | -0 17.68 | | 48960.2 | 18029.6 | 45519.2 | +0.4 | |
| | 26 | | -0 17.29 | | 48960.3 | 18029.3 | 45519.1 | +0.7 | |
| Aug. | 2 | | -0 17.52 | | 48960.6 | 18029.9 | 45519.1 | +0.8 | |
| | 9 | | -0 17.46 | | 48960.4 | 18031.3 | 45518.9 | +0.2 | |
| | 16 | -0 17.30 | -0 17.38 | +68 23.46 | 48960.1 | 18030.7 | 45519.2 | -0.1 | +0.01 |
| | 23 | | -0 17.41 | | 48960.4 | 18030.0 | 45519.0 | +0.6 | |
| | 30 | | -0 17.48 | | 48959.8 | 18030.7 | 45518.9 | -0.1 | |
| Sep. | 6 | | -0 17.59 | | 48960.3 | 18031.0 | 45519.2 | +0.0 | |
| | 13 | | -0 17.45 | | 48960.3 | 18030.2 | 45519.0 | +0.4 | |
| | 20 | | -0 17.15 | | 48960.4 | 18030.5 | 45519.2 | +0.2 | |
| | 27 | -0 17.34 | -0 17.61 | +68 23.39 | 48960.6 | 18030.7 | 45518.9 | +0.7 | -0.06 |
| Oct. | 5 | | -0 17.38 | | 48960.1 | 18030.6 | 45518.8 | +0.3 | |
| | 11 | | -0 17.44 | | 48960.6 | 18030.6 | 45519.2 | +0.4 | |
| | 18 | | -0 17.52 | | 48961.3 | 18029.9 | 45519.7 | +0.9 | |
| | 25 | -0 17.59 | -0 17.55 | +68 23.50 | 48961.0 | 18030.1 | 45519.5 | +0.7 | +0.00 |
| Nov. | 1 | | -0 17.47 | | 48961.5 | 18030.2 | 45519.5 | +1.2 | |
| | 8 | | -0 17.54 | | 48961.1 | 18030.5 | 45519.5 | +0.7 | |
| | 15 | | -0 17.46 | | 48961.2 | 18030.0 | 45519.8 | +0.7 | |
| | 22 | | -0 17.39 | | 48961.0 | 18030.5 | 45519.6 | +0.5 | |
| | 29 | -0 17.50 | -0 17.03 | +68 23.58 | 48961.3 | 18030.6 | 45519.8 | +0.6 | +0.10 |
| Dec. | 6 | | -0 17.36 | | 48961.0 | 18030.5 | 45519.6 | +0.5 | |
| | 13 | | -0 17.30 | | 48961.2 | 18030.3 | 45519.4 | +0.9 | |
| | 20 | | -0 17.17 | | 48960.8 | 18030.3 | 45519.5 | +0.4 | |
| | 27 | -0 17.42 | -0 17.35 | +68 23.47 | 48961.3 | 18029.9 | 45519.9 | +0.7 | -0.05 |

Table 1 Wingst 2000 base line values of the fluxgate system FGE125

Wingst (WNG)

Geographic Coordinates: 53.743° N 9.073° E

2000

Monthly mean values, IMS

D: disturbed, Q: quiet, A: all days

| Month | | D | F nT | H nT | I | X nT | Y nT | Z nT |
|-------|---|-------|---------|---------|----------|---------|---------|---------|
| Jan | A | 12.3' | 49115 | 18060 | 68°25.6' | 18060 | 64 | 45674 |
| Feb | A | 12.5 | 49118 | 18060 | 68 25.6 | 18060 | 66 | 45677 |
| Mar | A | 12.7 | 49118 | 18069 | 68 24.9 | 18069 | 67 | 45673 |
| Apr | A | 14.3 | 49120 | 18061 | 68 25.6 | 18061 | 75 | 45679 |
| May | A | 14.3 | 49123 | 18073 | 68 24.8 | 18073 | 75 | 45678 |
| Jun | A | 14.6 | 49131 | 18076 | 68 24.8 | 18076 | 77 | 45685 |
| Jul | A | 15.7 | 49134 | 18067 | 68 25.5 | 18067 | 82 | 45692 |
| Aug | A | 16.2 | 49138 | 18064 | 68 25.9 | 18064 | 85 | 45697 |
| Sep | A | 17.4 | 49139 | 18060 | 68 26.2 | 18060 | 91 | 45700 |
| Oct | A | 18.0 | 49146 | 18055 | 68 26.8 | 18055 | 94 | 45709 |
| Nov | A | 18.4 | 49149 | 18058 | 68 26.6 | 18058 | 97 | 45712 |
| Dec | A | 18.3 | 49150 | 18070 | 68 25.8 | 18070 | 96 | 45708 |
| Mean | A | 15.4 | 49132 | 18064 | 68 25.7 | 18064 | 81 | 45690 |
| Jan | Q | 11.4 | 49116 | 18068 | 68 25.0 | 18068 | 60 | 45672 |
| Feb | Q | 12.0 | 49119 | 18068 | 68 25.1 | 18068 | 63 | 45676 |
| Mar | Q | 12.4 | 49118 | 18074 | 68 24.6 | 18074 | 65 | 45672 |
| Apr | Q | 13.5 | 49122 | 18071 | 68 24.9 | 18071 | 71 | 45677 |
| May | Q | 13.9 | 49123 | 18081 | 68 24.2 | 18081 | 73 | 45674 |
| Jun | Q | 15.3 | 49130 | 18074 | 68 24.9 | 18074 | 80 | 45685 |
| Jul | Q | 15.2 | 49133 | 18075 | 68 24.9 | 18075 | 80 | 45687 |
| Aug | Q | 16.0 | 49136 | 18071 | 68 25.3 | 18071 | 84 | 45692 |
| Sep | Q | 16.5 | 49138 | 18070 | 68 25.4 | 18070 | 87 | 45695 |
| Oct | Q | 17.6 | 49147 | 18062 | 68 26.3 | 18062 | 93 | 45708 |
| Nov | Q | 17.5 | 49149 | 18072 | 68 25.6 | 18072 | 92 | 45705 |
| Dec | Q | 18.2 | 49149 | 18077 | 68 25.3 | 18077 | 96 | 45705 |
| Mean | Q | 15.0 | 49132 | 18072 | 68 25.1 | 18072 | 79 | 45687 |
| Jan | D | 13.7 | 49112 | 18050 | 68 26.2 | 18050 | 72 | 45675 |
| Feb | D | 13.4 | 49117 | 18046 | 68 26.7 | 18046 | 70 | 45682 |
| Mar | D | 13.2 | 49119 | 18059 | 68 25.7 | 18059 | 70 | 45679 |
| Apr | D | 16.7 | 49115 | 18036 | 68 27.3 | 18036 | 88 | 45684 |
| May | D | 15.2 | 49120 | 18059 | 68 25.7 | 18059 | 80 | 45679 |
| Jun | D | 13.7 | 49135 | 18081 | 68 24.5 | 18081 | 72 | 45687 |
| Jul | D | 17.3 | 49133 | 18049 | 68 26.9 | 18049 | 91 | 45698 |
| Aug | D | 17.1 | 49137 | 18046 | 68 27.2 | 18046 | 89 | 45704 |
| Sep | D | 19.0 | 49135 | 18044 | 68 27.3 | 18044 | 100 | 45703 |
| Oct | D | 19.5 | 49144 | 18027 | 68 28.8 | 18027 | 102 | 45719 |
| Nov | D | 20.0 | 49145 | 18031 | 68 28.6 | 18031 | 105 | 45718 |
| Dec | D | 18.3 | 49148 | 18065 | 68 26.0 | 18065 | 96 | 45708 |
| Mean | D | 16.4 | 49130 | 18049 | 68 26.7 | 18049 | 86 | 45695 |

Table 2 Monthly and annual mean values 2000
Wingst (WNG)

Geographic Coordinates: 53.743°N 9.073°E

Annual mean values (IMS)

| Epoch | D | F nT | H nT | I | X nT | Y nT | Z nT |
|--------|----------|---------|---------|----------|---------|---------|---------|
| 1939.5 | -5°59.1' | 47476 | 17630 | 68°12.1' | 17534 | -1838 | 44081 |
| 1940.5 | -5 50.2 | 47506 | 17624 | 68 13.4 | 17533 | -1792 | 44116 |
| 1941.5 | -5 40.8 | 47550 | 17617 | 68 15.2 | 17530 | -1744 | 44166 |
| 1942.5 | -5 33.1 | 47579 | 17622 | 68 15.7 | 17540 | -1705 | 44196 |
| 1943.5 | -5 24.2 | 47634 | 17614 | 68 18.0 | 17535 | -1659 | 44259 |
| 1944.5 | -5 16.2 | 47652 | 17616 | 68 18.3 | 17541 | -1618 | 44276 |
| 1945.5 | -5 8.2 | 47671 | 17611 | 68 19.2 | 17540 | -1577 | 44299 |
| 1946.5 | -4 59.6 | 47708 | 17595 | 68 21.5 | 17528 | -1532 | 44346 |
| 1947.5 | -4 51.7 | 47726 | 17596 | 68 22.0 | 17532 | -1491 | 44365 |
| 1948.5 | -4 44.4 | 47775 | 17602 | 68 22.9 | 17541 | -1454 | 44415 |
| 1949.5 | -4 36.6 | 47791 | 17604 | 68 23.2 | 17547 | -1415 | 44431 |
| 1950.5 | -4 29.1 | 47814 | 17617 | 68 22.9 | 17562 | -1378 | 44451 |
| 1951.5 | -4 21.5 | 47832 | 17624 | 68 22.8 | 17573 | -1339 | 44468 |
| 1952.5 | -4 14.5 | 47861 | 17636 | 68 22.7 | 17587 | -1304 | 44494 |
| 1953.5 | -4 7.6 | 47882 | 17653 | 68 22.0 | 17607 | -1270 | 44510 |
| 1954.5 | -4 1.3 | 47899 | 17666 | 68 21.5 | 17623 | -1239 | 44523 |
| 1955.5 | -3 55.1 | 47930 | 17676 | 68 21.6 | 17634 | -1208 | 44552 |
| 1956.5 | -3 49.3 | 47964 | 17676 | 68 22.6 | 17636 | -1178 | 44589 |
| 1957.5 | -3 44.2 | 47993 | 17686 | 68 22.6 | 17648 | -1152 | 44616 |
| 1958.5 | -3 39.5 | 48023 | 17700 | 68 22.4 | 17663 | -1129 | 44643 |
| 1959.5 | -3 34.6 | 48062 | 17714 | 68 22.4 | 17679 | -1105 | 44679 |
| 1960.5 | -3 30.1 | 48095 | 17727 | 68 22.4 | 17693 | -1082 | 44710 |
| 1961.5 | -3 25.7 | 48117 | 17751 | 68 21.1 | 17719 | -1061 | 44723 |
| 1962.5 | -3 21.3 | 48136 | 17773 | 68 20.0 | 17742 | -1040 | 44735 |
| 1963.5 | -3 16.9 | 48160 | 17789 | 68 19.4 | 17760 | -1018 | 44755 |
| 1964.5 | -3 13.1 | 48183 | 17810 | 68 18.4 | 17782 | -1000 | 44771 |
| 1965.5 | -3 9.6 | 48201 | 17829 | 68 17.5 | 17802 | -983 | 44783 |
| 1966.5 | -3 6.3 | 48226 | 17842 | 68 17.3 | 17815 | -966 | 44805 |
| 1967.5 | -3 3.4 | 48254 | 17855 | 68 17.1 | 17829 | -952 | 44830 |
| 1968.5 | -3 1.0 | 48286 | 17874 | 68 16.5 | 17849 | -941 | 44857 |
| 1969.5 | -2 59.2 | 48320 | 17899 | 68 15.5 | 17874 | -932 | 44883 |
| 1970.5 | -2 56.9 | 48359 | 17924 | 68 14.7 | 17900 | -922 | 44915 |
| 1971.5 | -2 54.5 | 48397 | 17953 | 68 13.6 | 17930 | -911 | 44944 |
| 1972.5 | -2 51.0 | 48434 | 17977 | 68 12.9 | 17954 | -894 | 44975 |
| 1973.5 | -2 46.6 | 48473 | 17999 | 68 12.2 | 17978 | -872 | 45008 |
| 1974.5 | -2 41.4 | 48513 | 18018 | 68 11.9 | 17998 | -846 | 45043 |
| 1975.5 | -2 36.0 | 48549 | 18043 | 68 11.0 | 18024 | -818 | 45073 |
| 1976.5 | -2 29.3 | 48583 | 18062 | 68 10.5 | 18045 | -784 | 45101 |
| 1977.5 | -2 22.4 | 48612 | 18078 | 68 10.1 | 18062 | -748 | 45126 |
| 1978.5 | -2 14.1 | 48646 | 18081 | 68 10.9 | 18066 | -705 | 45161 |
| 1979.5 | -2 6.3 | 48668 | 18089 | 68 10.9 | 18076 | -664 | 45181 |
| 1980.5 | -1 59.0 | 48682 | 18096 | 68 10.7 | 18085 | -626 | 45194 |
| 1981.5 | -1 51.4 | 48704 | 18091 | 68 11.7 | 18082 | -586 | 45220 |
| 1982.5 | -1 43.9 | 48724 | 18084 | 68 12.8 | 18076 | -546 | 45244 |
| 1983.5 | -1 36.9 | 48738 | 18087 | 68 13.0 | 18080 | -510 | 45257 |
| 1984.5 | -1 29.9 | 48752 | 18083 | 68 13.7 | 18077 | -473 | 45274 |
| 1985.5 | -1 23.5 | 48768 | 18080 | 68 14.4 | 18075 | -439 | 45292 |
| 1986.5 | -1 17.0 | 48787 | 18071 | 68 15.5 | 18067 | -404 | 45316 |
| 1987.5 | -1 11.1 | 48804 | 18069 | 68 16.2 | 18065 | -374 | 45336 |
| 1988.5 | -1 5.0 | 48829 | 18056 | 68 17.9 | 18053 | -341 | 45368 |
| 1989.5 | -59.0 | 48856 | 18042 | 68 19.7 | 18039 | -309 | 45402 |
| 1990.5 | -53.9 | 48875 | 18041 | 68 20.3 | 18038 | -283 | 45423 |
| 1991.5 | -48.5 | 48895 | 18032 | 68 21.5 | 18031 | -255 | 45448 |
| 1992.5 | -43.4 | 48911 | 18038 | 68 21.5 | 18037 | -228 | 45463 |
| 1993.5 | -37.1 | 48928 | 18044 | 68 21.6 | 18043 | -195 | 45479 |
| 1994.5 | -30.0 | 48952 | 18045 | 68 22.2 | 18044 | -158 | 45505 |
| 1995.5 | -23.0 | 48975 | 18053 | 68 22.2 | 18053 | -121 | 45526 |
| 1996.5 | -15.6 | 48998 | 18062 | 68 22.1 | 18062 | -82 | 45547 |
| 1997.5 | -7.6 | 49028 | 18063 | 68 22.9 | 18063 | -40 | 45579 |
| 1998.5 | 0.5 | 49062 | 18059 | 68 24.2 | 18059 | 3 | 45618 |
| 1999.5 | 8.0 | 49094 | 18063 | 68 24.7 | 18063 | 42 | 45651 |
| 2000.5 | 15.4 | 49132 | 18064 | 68 25.7 | 18064 | 81 | 45690 |

Table 3 Wingst Epoch values from 1939 to 2000

Wingst (WNG)

Geographic Coordinates: 53.743°N 9.073°E

2000

Absolute and relative Frequencies of the Three-hourly Index K

| K | UTC | 0-3 | 3-6 | 6-9 | 9-12 | 12-15 | 15-18 | 18-21 | 21-24 |
|---|-----|-----|-----|-----|------|-------|-------|-------|-------|
| 0 | | 24 | 24 | 7 | 7 | 2 | 12 | 10 | 14 |
| 1 | | 59 | 63 | 103 | 76 | 61 | 59 | 51 | 38 |
| 2 | | 100 | 117 | 135 | 123 | 128 | 105 | 95 | 104 |
| 3 | | 100 | 107 | 81 | 116 | 102 | 93 | 106 | 95 |
| 4 | | 53 | 34 | 28 | 33 | 49 | 58 | 48 | 78 |
| 5 | | 19 | 16 | 9 | 7 | 14 | 25 | 42 | 27 |
| 6 | | 7 | 5 | 2 | 4 | 9 | 10 | 8 | 7 |
| 7 | | 3 | 0 | 1 | 0 | 1 | 3 | 4 | 0 |
| 8 | | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |
| 9 | | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 3 |

Absolute Number of Days during the Year for a given K

| K | Jan | Feb | Mar | Apr | May | Jun | Jul | Aug | Sep | Oct | Nov | Dec | Year |
|---|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|
| 0 | 13 | 8 | 19 | 7 | 1 | 1 | 0 | 7 | 7 | 7 | 10 | 20 | 100 |
| 1 | 41 | 38 | 62 | 38 | 19 | 30 | 27 | 34 | 25 | 55 | 56 | 85 | 510 |
| 2 | 81 | 63 | 78 | 81 | 100 | 71 | 76 | 77 | 77 | 68 | 56 | 79 | 907 |
| 3 | 62 | 57 | 70 | 71 | 71 | 74 | 79 | 74 | 67 | 67 | 60 | 48 | 800 |
| 4 | 33 | 40 | 16 | 33 | 37 | 41 | 34 | 33 | 40 | 28 | 34 | 12 | 381 |
| 5 | 14 | 23 | 3 | 6 | 16 | 16 | 20 | 17 | 14 | 9 | 17 | 4 | 159 |
| 6 | 4 | 3 | 0 | 0 | 3 | 7 | 5 | 5 | 8 | 11 | 6 | 0 | 52 |
| 7 | 0 | 0 | 0 | 1 | 1 | 0 | 4 | 1 | 1 | 3 | 1 | 0 | 12 |
| 8 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| 9 | 0 | 0 | 0 | 2 | 0 | 0 | 3 | 0 | 1 | 0 | 0 | 0 | 6 |

Absolute Number of Three-hour-intervals for a given K

Table 4 Statistics of indices 2000

Appendix 3: On the calculation of base-line values using definitive variations

1. Co-ordinate systems

At Wingst Observatory, the elements D , I , F , Z , Nelson's H and Serson's D are measured using a DI-flux and a PVM (VOPPEL, 1972; SCHULZ, 1981), respectively. On the other hand, variations of the geomagnetic components are recorded by fluxgates aligned towards the co-ordinates U , V and Z , which differ from the geographic co-ordinates X , Y and Z . This system, which is also Cartesian, is derived from the geographic system by 45° counter-clockwise rotation on the horizontal plane (from N to NE). Advantage: due to the small declination at Wingst, both horizontal components U and V are equally included in the difference between the recorded and calculated F .

X (N) and Y (E) can be calculated from the recorded components U (NW) and V (NE) as follows:

$$(1) \quad X = a(U+V) \text{ and } Y = a(V-U), \text{ with } a = \sqrt{2}/2$$

They are analytically connected with the polar co-ordinates D and H :

$$(2) \quad D = \text{atan}(Y/X) \text{ and } H = \sqrt{X^2+Y^2}$$

Generally, the following applies to the base-line values B_0 :

$$(3) \quad B_0 = B-b, \text{ with}$$

$$\begin{array}{ll} B = X, Y, Z, H, D, I \text{ or } F & \text{for the elements, and} \\ b = x, y, z, h, d, i \text{ or } f & \text{for the corresponding variations.} \end{array}$$

Relation (1) applies also to the variations:

$$x = a(u+v) \text{ and } y = a(v-u).$$

2. Determination of definitive variations:

There are two major advantages to having definitive variations available:

Base-line measurements of different elements can be carried out consecutively – and, if appropriate, independently at the same location. In the latter case, the determination of differences between two locations is not necessary.

The readings can be reduced individually according to the variations of the element measured. Freed from external parts, the quality of the readings can be easily checked and outliers detected by assessing their scattering at a given coil/sensor position.

a) *D, I, F and Nelson's H:*

The elements *D, I, F, Z* and *H* are measured using a DI-flux and a PVM (compensation field method), respectively. The corresponding variations *d, i, f* and *h* have to be calculated from these elements and from the variations *x, y* and *z*. In order to obtain definitive values, this can be done by developing relation (2) according to Taylor's rule within the range of variations up to terms of second order. The results of the latest base-line measurements can be inserted for the coefficients according to (3). The following applies to the elements on the horizontal plane (*d* and *i* in radians):

$$(4a) \quad \begin{aligned} h &= 1/H[Xx+Yy+0.5(1-X^2/H^2)x^2+0.5(1-Y^2/H^2)y^2-(XY/H^2)xy] \\ d &= 1/H^2 [Xy-Yx-XY/H^2(x^2-y^2)-((Y^2-X^2)/H^2)xy] \end{aligned}$$

Correspondingly, the following applies to the magnetic meridian:

$$(4b) \quad \begin{aligned} f &= 1/F[Hh+Zz+0.5(1-H^2/F^2)h^2+0.5(1-Z^2/F^2)z^2-(HZ/F^2)hz] \\ i &= 1/F^2 [Hz-Zh-HZ/F^2(h^2-z^2)-((Z^2-H^2)/F^2)hz] \end{aligned}$$

Even for strong variations (storm), higher terms do not have to be added. They seldom exceed the relative order of magnitude of 10^{-3} .

B-b

are the readings of the elements referred to the respective coil/sensor position, freed from external parts.

b) *Serson's D:*

The readings *S* of Serson's *D* (PVM, addition field method) can be developed in the same manner. They are given by

$$(5) \quad \begin{aligned} S_1^2 &= Z^2+H^2+A^2-2HA\sin(d) \text{ and} \\ S_2^2 &= Z^2+H^2+A^2+2HA\sin(d). \end{aligned}$$

The horizontal bias field *A* is either directed eastward (index 1) or westward (index 2), respectively. Applying Taylor's rule, the following expressions can be used to reduce the readings (5)

$$\begin{aligned} s_1 &= 1/S\{Zz+Hh-HAd-0.5/S^2[(S^2-Z^2)z^2+(S^2-H^2)h^2-H^2A^2d^2]+HZhz-HAZzd-H^2Ahd\} \\ \text{and} \\ s_2 &= 1/S\{Zz+Hh+HAd-0.5/S^2[(S^2-Z^2)z^2+(S^2-H^2)h^2-H^2A^2d^2]+HZhz+HAZzd+H^2Ahd\}, \end{aligned}$$

respectively.

Half the difference α in the sense 1 minus 2 is the small correction which has to be applied to the fixed nominal position on the horizontal circle to get the base-line of Serson's D referred to the respective coil position:

$$\alpha = S/(2HA)[S_{01}-S_{02}]$$

c) *A more simple routine for D, I, F and H:*

Going back to the elements D , I , F and H , the following simplification provides an faster method from the programmer's point of view. It corresponds to the quadratic solutions (4), but only linear terms are taken into account. Index 1 denotes the terms developed at the positions of the base-line values B_0 most recently calculated, index 2 those at the measured elements :

$$\begin{aligned} d_1 &= 1/H_0^2(X_0y - Y_0x) & d_2 &= 1/H^2(-Xy + Yx) \\ i_1 &= 1/F_0^2(H_0z - Z_0h) & i_2 &= 1/F^2(-Hz + Zh) \\ f_1 &= 1/F_0(H_0h + Z_0z) & f_2 &= 1/F(-Hh - Zz) \\ h_1 &= 1/H_0(X_0x + Y_0y) & h_2 &= 1/H(-Xx - Yy) \end{aligned}$$

In this way, half the differences in the sense 1 minus 2

$$b = 1/2(b_1 - b_2)$$

are sufficiently accurate and can also be considered definitive.

References:

SCHULZ, G. 1981: Base-line measurements of the declination, by means of a proton vector magnetometer, at Wingst Observatory (Erdmagnetisches Observatorium Wingst). Dt. hydrogr. Z. 34, 26-37

VOPPEL, D. 1972: The proton vector magnetometer at Wingst Observatory – technical data and application. Erdmagn. Jahrb. Nr 17, 133-149